

MATHEMATICS CURRICULUM PROJECT

GOAL 9: Use geometric methods to analyze, categorize and draw conclusions about points, lines, planes and space.

Standard A: Demonstrate and apply geometric concepts involving points, lines, planes and space.

*As a result of their schooling students will be able to...*

Kindergarten	Grade 1	Grade 2	Grade 3	Grade 4
<ol style="list-style-type: none"> <li>1. Identify circle, square, triangle and rectangle.</li> <li>2. Begin to recognize other shapes of objects.</li> <li>3. Explore three-dimensional shapes.</li> </ol>	<ol style="list-style-type: none"> <li>1. Identify two- and three-dimensional shapes.</li> <li>2. Model two-dimensional geometric shapes by drawing or building.</li> <li>3. Describe and interpret relative positions in space and apply concepts of relative position (e.g., above/below).</li> <li>4. Recognize and describe shapes that have line symmetry.</li> <li>5. Identify geometric shapes and structures in the environment.</li> <li>6. Explore the effects of translations (slides), reflections (flips) and rotations (turns) with concrete objects.</li> </ol>	<ol style="list-style-type: none"> <li>1. Investigate and predict the results of putting together and taking apart two- and three-dimensional shapes (e.g., put two triangles together to make a quadrilateral).</li> <li>2. Describe and interpret direction and distance in navigating space and apply concepts of direction and distance (e.g., nearer/farther).</li> <li>3. Perform translations (slides), reflections (flips) and rotations (turns) with concrete objects.</li> <li>4. Create and complete shapes that have line symmetry.</li> </ol>	<ol style="list-style-type: none"> <li>1. Find and name two- and three-dimensional geometric figures in every day objects.</li> <li>2. Identify the properties, number of sides and corners of geometric shapes.</li> <li>3. Draw two-dimensional shapes using rulers, graphing paper and tracing paper.</li> <li>4. Visualize the transition from two-dimensional to its three-dimensional figure.</li> <li>5. Construct three-dimensional geometric figures.</li> <li>6. Locate and identify points using numbers and symbols on a grid and describe how points relate to each other on a grid.</li> </ol>	<ol style="list-style-type: none"> <li>1. Identify, draw and label lines, line segments, rays, parallel lines, intersecting lines, perpendicular lines, acute angles, obtuse angles, right angles and acute, obtuse, right, scalene, isosceles and equilateral triangles.</li> <li>2. Identify, draw and build regular and irregular polygons.</li> <li>3. Read and plot ordered pairs of numbers in the positive quadrant of the Cartesian plane.</li> <li>4. Describe paths and movement using coordinate systems.</li> <li>5. Differentiate between polygons and non-polygons.</li> <li>6. Identify and label radius and diameter of a circle.</li> <li>7. Explore and describe rotational symmetry of two- and three-dimensional shapes.</li> <li>8. Construct a circle with a specified radius or diameter using a compass.</li> </ol>

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<ol style="list-style-type: none"> <li>1. Identify, compare and analyze attributes of two- and three-dimensional shapes and develop vocabulary to describe the attributes.</li> <li>2. Classify two- or three-dimensional shapes according to their properties (e.g., regular and irregular types of quadrilaterals, pyramids and prisms).</li> <li>3. Investigate and describe the results of subdividing and combining shapes.</li> <li>4. Describe paths using coordinate systems.</li> <li>5. Determine the distance between points along horizontal and vertical lines of a coordinate system.</li> <li>6. Identify and justify rotational symmetry in two- and three-dimensional shapes.</li> <li>7. Identify and describe how geometric figures are used in practical settings (e.g., construction, art, advertising, architecture).</li> <li>8. Identify and label radius, diameter, chord and circumference of a circle.</li> <li>9. Copy a line segment or an angle using a straightedge and a compass.</li> <li>10. Construct angles and perpendicular bisectors of line segments.</li> <li>11. Solve problems using properties of triangles (e.g., sum of interior angles of a triangle is <math>180^\circ</math>).</li> </ol>	<ol style="list-style-type: none"> <li>1. Plot and read ordered pairs of numbers in all four quadrants.</li> <li>2. Describe sizes, positions and orientations of shapes under transformations, including dilations.</li> <li>3. Perform simple constructions (e.g., equal segments, angle and segment bisectors, or perpendicular lines, inscribing a hexagon in a circle) with a compass and straightedge or a mira.</li> <li>4. Determine and describe the relationship between pi, the diameter, the radius and the circumference of a circle.</li> <li>5. Determine unknown angle measures using angle relationships and properties of a triangle or a quadrilateral.</li> </ol>	<ol style="list-style-type: none"> <li>1. Examine and describe a geometric shape, such as a regular polygon or a quadrilateral with pairs of parallel or perpendicular sides, using coordinate geometry.</li> <li>2. Draw geometric shapes with specified properties, such as side lengths or angle measures.</li> <li>3. Examine and describe line or rotational symmetry of objects in terms of transformations.</li> <li>4. Draw transformations of figures in a plane to match specified criteria.</li> <li>5. Perform constructions of congruent angles or parallel lines using a compass and straightedge, paper folding, or a mira.</li> <li>6. Determine the relationship among the number of edges, faces and vertices in a three-dimensional object.</li> </ol>	<ol style="list-style-type: none"> <li>1. Solve problems involving two- and three-dimensional shapes.</li> <li>2. Apply and use the Pythagorean Theorem.</li> <li>3. Identify, describe and determine the radius, diameter and circumference of a circle and their relationship to each other and to pi.</li> <li>4. Graph points and identify coordinates of points on the Cartesian coordinate plane.</li> <li>5. Represent and identify geometric figures using coordinate geometry.</li> <li>6. Use transformations in a Cartesian coordinate plane.</li> <li>7. Identify relationships of angles formed by intersecting lines.</li> <li>8. Solve problems involving vertical, complementary and supplementary angles.</li> </ol>

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GOAL 9: Use geometric methods to analyze, categorize and draw conclusions about points, lines, planes and space.

Standard B: Identify, describe, classify and compare relationships using points, lines, planes, and solids.

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Kindergarten	Grade 1	Grade 2	Grade 3	Grade 4
1. Identify and sort objects according to their shape.	<ol style="list-style-type: none"> <li>1. Identify objects that are the same shape.</li> <li>2. Compare and sort two- and three-dimensional objects.</li> <li>3. Compare and contrast sides and corners of basic geometric shapes.</li> </ol>	<ol style="list-style-type: none"> <li>1. Identify objects that are congruent</li> <li>2. Compare and contrast attributes of two- and three-dimensional objects using appropriate vocabulary.</li> </ol>	<ol style="list-style-type: none"> <li>1. Identify parallel and intersecting lines.</li> <li>2. Identify polygons v. non-polygons by defining components.</li> <li>3. Recognize and identify symmetrical figures with one and two lines of symmetry.</li> <li>4. Identify congruent figures in different positions.</li> <li>5. Identify similar figures that are not congruent and tell how they are similar.</li> </ol>	<ol style="list-style-type: none"> <li>1. Determine congruence and similarity of given shapes.</li> <li>2. Explore polyhedra (three-dimensional figures) using concrete models.</li> </ol>

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Grade 5	Grade 6	Grade 7	Grade8/Pre-Algebra/Algebra
<ol style="list-style-type: none"> <li>1. Demonstrate congruence of plane figures using transformations (translation, rotation, reflection).</li> <li>2. Determine if two polygons are congruent using measures of angles and sides.</li> <li>3. Match a front, right side and top view drawing with a three-dimensional model built with cubes.</li> </ol>	<ol style="list-style-type: none"> <li>1. Determine the relationships between the number of vertices or sides in a polygon, the number of diagonals and the sum of its angles.</li> <li>2. Analyze quadrilaterals for defining characteristics.</li> <li>3. Create a three-dimensional object from any two-dimensional representation of the object, including multiple views, nets, or technological representations.</li> <li>4. Identify and describe the five regular polyhedra.</li> <li>5. Create regular and semi-regular tessellations using pattern blocks, other manipulatives or technology to tile a plane.</li> </ol>	<ol style="list-style-type: none"> <li>1. Describe, classify and justify relationships among types of two- and three-dimensional objects using their defining properties.</li> <li>2. Solve problems using properties of polygons and circles.</li> <li>3. Classify and order quadrilaterals according to their properties.</li> </ol>	<ol style="list-style-type: none"> <li>1. Identify front, side and top views of a three-dimensional solid built with cubes.</li> <li>2. Solve problems involving congruent and similar figures.</li> <li>3. Relate absolute value to distance on the number line.</li> </ol>

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GOAL 9: Use geometric methods to analyze, categorize and draw conclusions about points, lines, planes and space.

Standard C: Construct convincing arguments and proofs to solve problems.

Standard D: Use trigonometric ratios and circular functions to solve problems (only applies to grades 7 & 8).

*As a result of their schooling students will be able to...*

Kindergarten	Grade 1	Grade 2	Grade 3	Grade 4
1. Verbally explain the different qualities of the shape of an object.	<ol style="list-style-type: none"> <li>1. Recognize and explain a geometric pattern.</li> <li>2. Verbalize the rule for the geometric pattern sequence (e.g., amount doubles).</li> </ol>	1. Justify an extension of a pattern.	<ol style="list-style-type: none"> <li>1. Verbally describe the properties of basic geometric figures.</li> <li>2. Create and explain patterns using pattern blocks and manipulatives.</li> </ol>	3. Make and test predictions about mathematical properties and relationships and justify the conclusions.

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Grade 5	Grade 6	Grade 7	Grade8/Pre-Algebra/Algebra
<ol style="list-style-type: none"> <li>1. Make and test conjectures about mathematical properties and relationships and develop logical arguments to justify conclusions.</li> <li>2. Make and test conjectures about the results of subdividing and combining shapes.</li> </ol>	<ol style="list-style-type: none"> <li>1. Make, test and justify conjectures about various quadrilateral and triangle relationships, including the triangle inequality.</li> <li>2. Justify the relationship between vertical angles.</li> <li>3. Justify that the sum of the angles of a triangle is 180 degrees.</li> </ol>	<ol style="list-style-type: none"> <li>1. Create and critique arguments about geometric relationships in figures based upon inductive and deductive reasoning.</li> <li>2. Justify the area formulas for triangles, parallelograms and trapezoids based on the formula for the area of a rectangle.</li> <li>3. Make and test conjectures about the relationships between side length and angle measure in various triangles and quadrilaterals.</li> <li>4. Justify the properties of angles formed by parallel lines cut by a transversal using appropriate terminology.</li> </ol> <p><u>Standard D</u></p> <ol style="list-style-type: none"> <li>1. Analyze the relationship between sides of right triangles using the Pythagorean theorem.</li> <li>2. Solve problems that involve the use of proportions and the Pythagorean theorem in similar right triangles with whole number side lengths.</li> </ol>	<ol style="list-style-type: none"> <li>1. Create and critique arguments concerning geometric ideas and relationships, such as congruence, similarity, the Pythagorean relationship, or formulas for surface areas or volume of simple three-dimensional objects.</li> <li>2. Represent, solve and explain numerical and algebraic relationships using geometric concepts.</li> <li>3. Provide examples or counter-examples to either illustrate or disprove conjectures about geometric characteristics.</li> </ol> <p><u>Standard D</u></p> <ol style="list-style-type: none"> <li>1. Recognize Pythagorean Triples.</li> <li>2. Identify the basic trigonometric ratio in terms of lengths of the sides of a right triangle and an acute angle.</li> </ol>